

8-6 Solving Rational Equations

Steps

*If the problem consists of one rational equaling one rational, cross multiply.
(Don't forget to FOIL / Distribute.)

1. Factor denominators and multiply EVERY fraction by the LCD (of ALL fractions). ex: $\frac{a}{d} + \frac{b}{d} = \frac{c}{d} \rightarrow$ multiply everything by $\frac{d}{1} = d$

**Remember Multiplying Fractions: $\frac{\text{Top} \cdot \text{Top}}{\text{Bottom} \cdot \text{Bottom}}$, so when the denominator of the LCD is 1, it is only necessary to multiply to the numerator.

2. Keep expressions in factored form \rightarrow cancel. There should be no more fractions.

3. Solve. Don't forget, you can solve quadratics by factoring / quadratic formula. Also include \pm when you take the square root of both sides of an equation.

4. Check your answer. For example, if you end up with $x=5$ and the original problem includes the expression $\frac{x}{x-5}$, there is "no solution" because it is impossible to divide by 0. $x=5$

Examples - Solve.

1. $\frac{3}{x} = \frac{12}{x+7}$

$$\begin{array}{r} 12x = 3x + 21 \\ -3x \quad -3x \\ \hline 9x = 21 \\ \frac{9x}{9} = \frac{21}{9} \\ x = \frac{7}{3} \end{array}$$

2. $x + \frac{6}{x} = -5x$

$$\begin{aligned} x^2 + 6 &= -5x \\ x^2 + 5x + 6 &= 0 \\ (x+3)(x+2) &= 0 \\ x &= -3, -2 \end{aligned}$$

3. $\frac{4 \cdot 3}{x+4} + \frac{5}{4} = \frac{18}{x+4}$

$$\begin{aligned} 12 + 5x + 20 &= 72 \\ 5x + 32 &= 72 \\ -32 \quad -32 \\ \hline 5x &= 40 \\ \frac{5x}{5} &= \frac{40}{5} \end{aligned}$$

4. $\frac{1}{b+1} + \frac{1}{b-1} = \frac{2}{b^2-1}$

$$\begin{aligned} b(-1) + b(1) &= 2 \\ \frac{2b}{2} &= \frac{2}{2} \\ b &= 1 \end{aligned}$$

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